

Computing the impact of central clearing on systemic risk

A Generative Approach

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joint work with Sharyn O'Halloran

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The views expressed in this presentation are those of the author alone.

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1 Introduction

2 Graph Model of Central Clearing

3 Stylized Case Studies

4 Generative Simulation Case Study

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The 07/08 Financial Crisis



- The 07/08 crisis challenged the fundamental assumption that **banks cannot fail**.
- Various big **regulatory changes** have been implemented such as collateralization and **central clearing**.

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- The 07/08 crisis challenged the fundamental assumption that **banks cannot fail**.
- Various big **regulatory changes** have been implemented such as collateralization and **central clearing**.
- Are we any safer today?
- How do we know that?

Empirical Data Analysis

- Now that the regulation has been implemented, an obvious approach to its evaluation is to **study empirical data ex-post**, e.g.:

Empirical Data Analysis

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- S. Ghamami and P. Glasserman. *Does OTC Derivatives Reform Incentivize Central Clearing?*. Journal of Financial Intermediation 32 (2017), pp. 76–87.
 - “Our dataset has reports from **five** of the ten largest U.S. banks ... We also have data on initial margin and guarantee fund contributions made by each bank **to 17 CCPs.**”
 - uses a macro-economic model
 - calibrated to empirical data

Evaluating the Impact of a Regulation

by empirical means

has the big

- **upside** that this is obviously of very **high practical relevance**.
- **downside** that empirical data is **invariably confounded** by many other factors.

by a generative approach

allows us to

- **compute the isolated impact** of a regulation before implementation.
- **model trade and risk relations** in a **clean graph model bridging the gap** between micro- and macro-economics.
- **illustrate** key drivers of impact in stylized case studies.
- **generate entire financial systems and compare impact**.

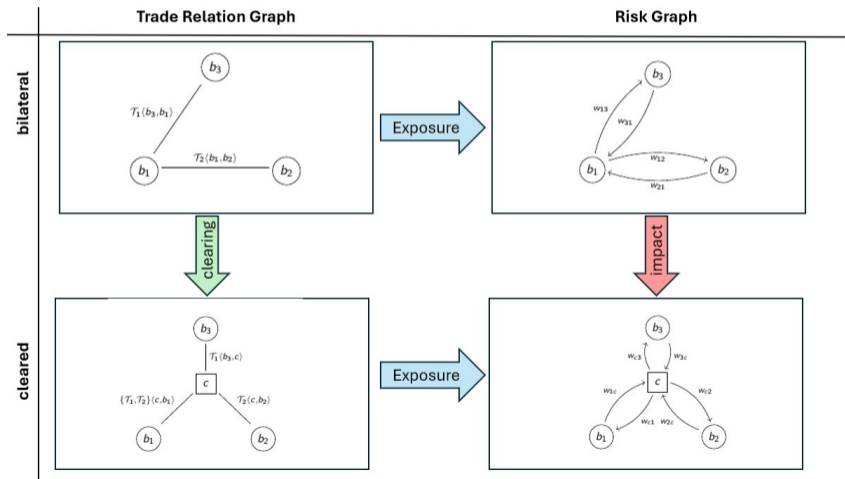
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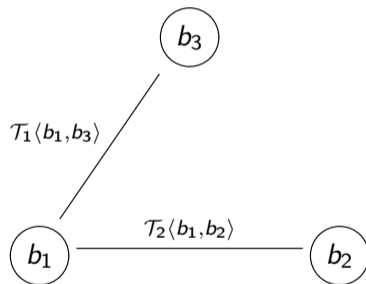
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Key Idea of Graph Model

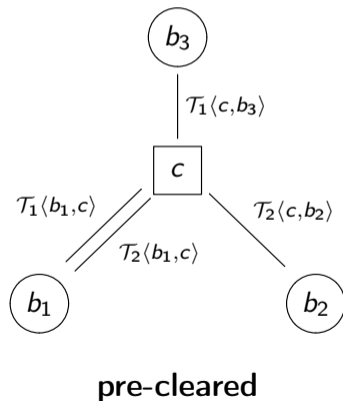
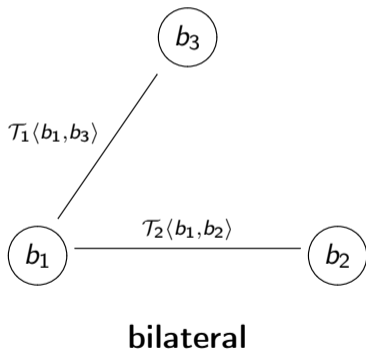


1. Pre-clearing

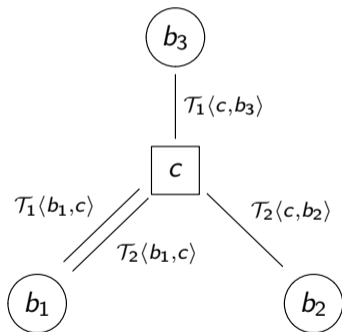


bilateral

1. Pre-clearing

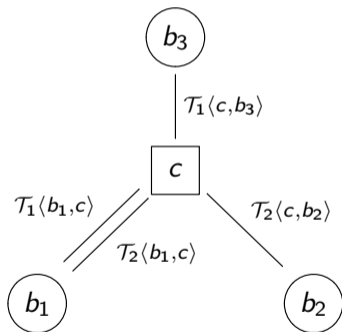


2. Compression

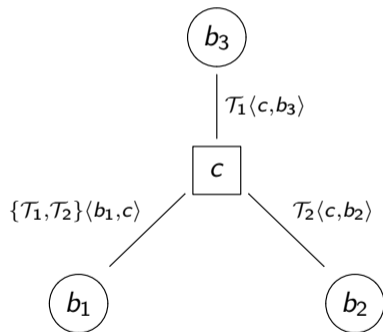


pre-cleared

2. Compression



pre-cleared

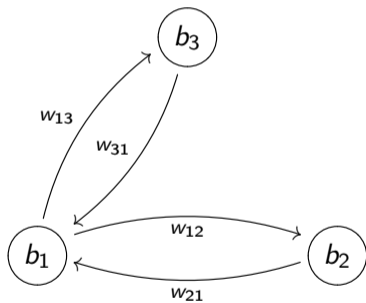


cleared

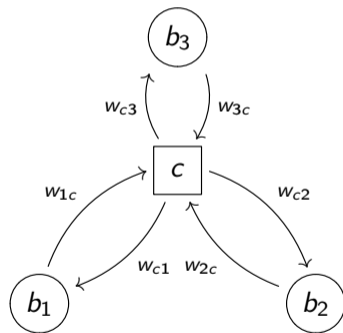
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Impact on Risk Graph



bilateral



cleared

Impact on Total Systemic Risk

#	operation	preserves netting	preserves adjacency	effect on system exposure
1.	pre-clearing	✓	✗	↑·2
2.	compression	✗	✓	↓·[0, 1]

- Total effect on total levels of exposure is interplay between competing effects of pre-clearing and compression.
- Hence, total effect is not obvious a priori.

Lower and upper bounds

Theorem

Let FS_{bil} be a bilateral financial system and FS_{clear} be the cleared system with a single CCP. Let

- w_{bil} be the total sum of all exposures in the bilateral system and
- w_{clear} be the total sum of all exposures in the cleared.

Then the cleared system has at most twice as much as the bilateral system:

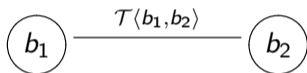
$$0 \leq w_{\text{clear}} \leq 2w_{\text{bil}}$$

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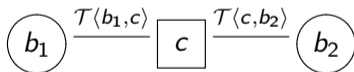
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Case: Two Banks: Double Exposure

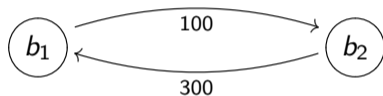
Trade Relation Graph FS (bilateral)



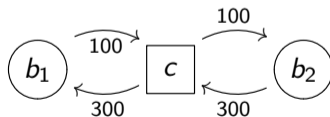
Trade Relation Graph \overline{FS} (cleared)



Risk Graph RG (bilateral)



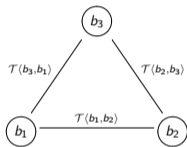
Risk Graph \overline{RG} (cleared)



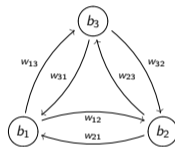
$$w_{\text{clear}} = 2w_{\text{bil}}$$

Case: Three Banks with a daisy chain: No Exposure

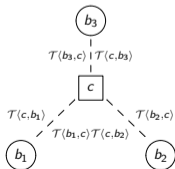
Trade Relation Graph FS (bilateral)



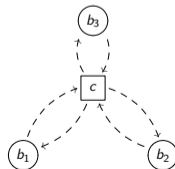
Risk Graph RG (bilateral)



Trade Relation Graph \overline{FS} (cleared)



Risk Graph \overline{RG} (cleared)



$$w_{\text{clear}} = 0$$

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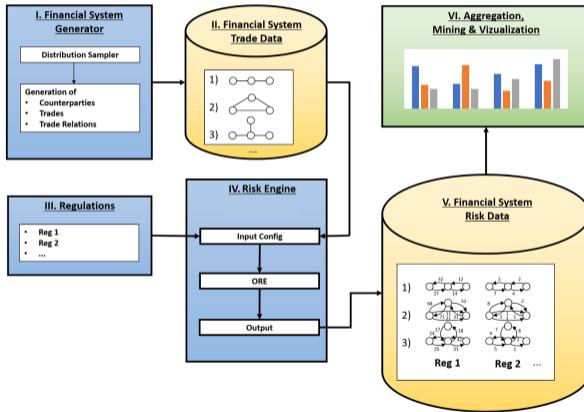
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The case for generative models

- **Real world impact** will be a mix of these stylized situations.
- Use of **real trade data** is **tempting** methodologically, but **impossible to carry out in practice**.
- Should the question whether or not a regulation has the desired impact **really depend on the precise trade data** as of today?
- **No!** We want the **impact of a regulation** to be **very robust** under many different scenarios (**avoid overfitting** regulation to current market).
- \implies Can use a **generative model** to create **synthetic data** of entire financial systems instead.

Generative Model: Impact of Regulation on Systemic Risk



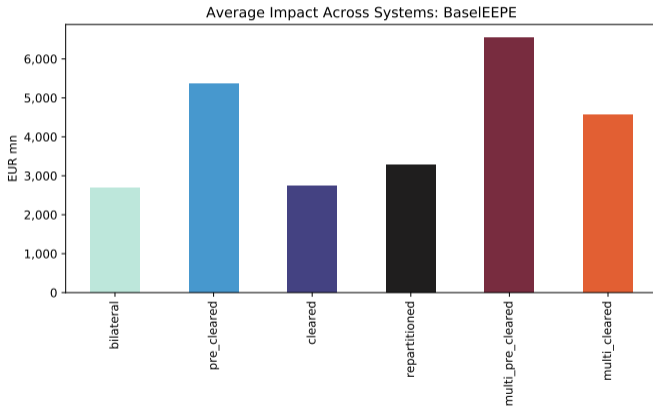
Technology Stack

- Python: lxml, numpy, networkx, pyvizjs, bqplot, matplotlib, seaborn, pandas, json, jupyter
- C++: boost, QuantLib, Open Source Risk Engine

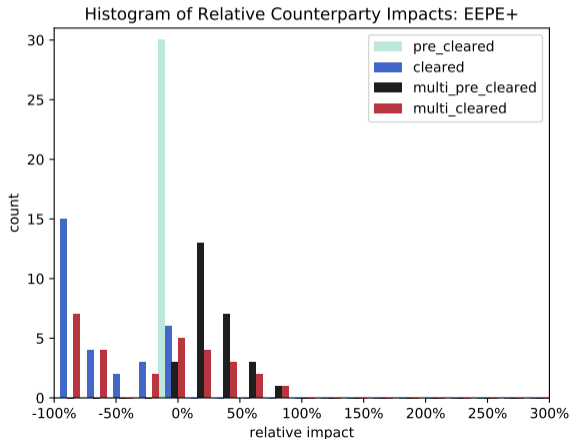
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Average Impacts across Systems (EEPE)

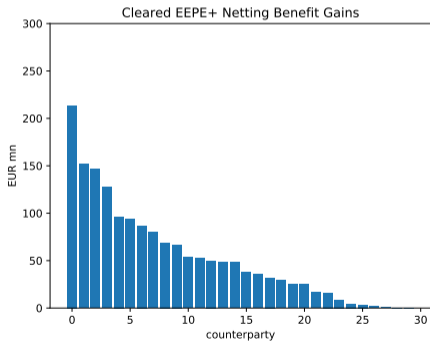


Histogram of Counterparty Impacts (EEPE)

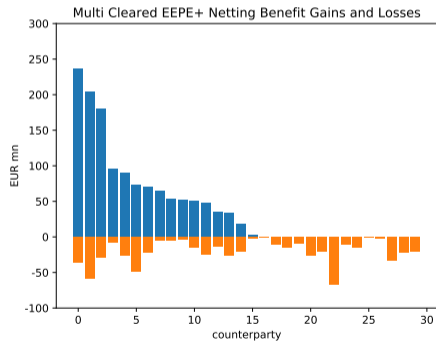


Netting Benefits (EEPE)

Single CCP



Multiple CCPs



Conclusion

- **Simulation case study based on generated financial systems confirms qualitative effects derived from theory and stylized case studies.**
- **Central clearing through single counterparty reduces exposure, but total impact of clearing through multiple CCPs is not unambiguously risk reducing.**
- **Results from abstract theory, stylized case studies, generative simulation case study and empirical research are broadly in line.**
- **Makes the case for the use of generative AI in financial regulation to**
 - **gauge impact of a regulation before implementation,**
 - **optimize** existing or future regulation,
 - **understand** impacts on a large scale.

References

Thank you!

- **Central Clearing:** Nowaczyk, Nikolai. O'Halloran, Sharyn. *Computing the impact of central clearing on systemic risk*. Front. Artif. Intell., 21 February 2024
<https://doi.org/10.3389/frai.2024.1138611>
- **Collateralization:** O'Halloran, Sharyn; Nowaczyk, Nikolai. *An Artificial Intelligence Approach to Regulating Systemic Risk*. Front. Artif. Intell., 29 May 2019
<https://doi.org/10.3389/frai.2019.00007>

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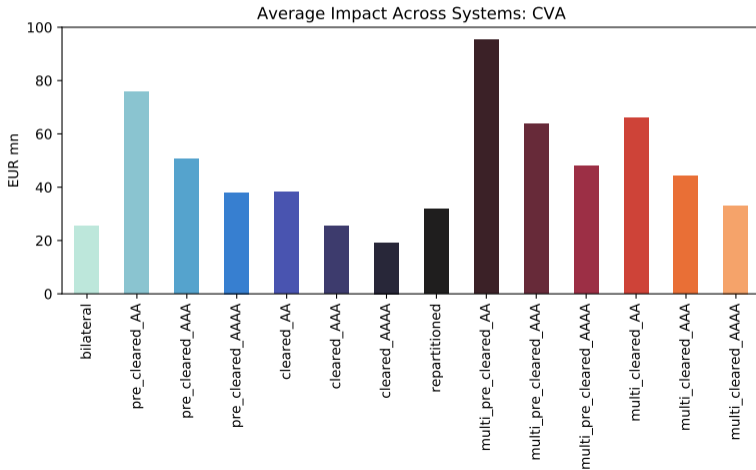
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 - CVA Impacts
 - Graph Model of Financial Systems

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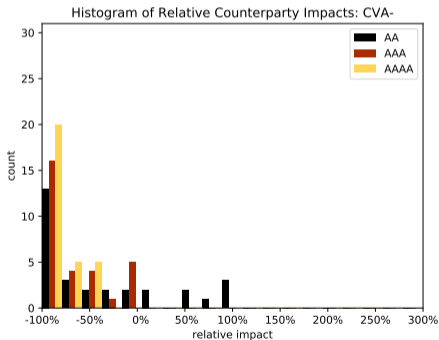
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Average Impacts across Systems (CVA)

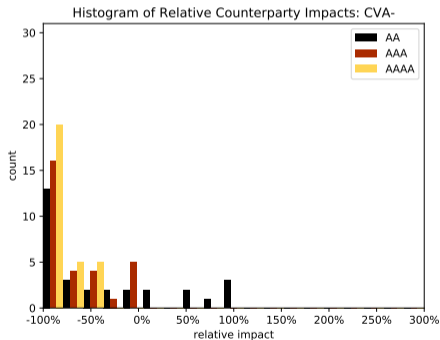


Absolute Impacts per Counterparty in System (CVA)

Single CCP



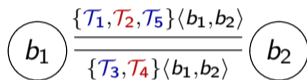
Multiple CCPs



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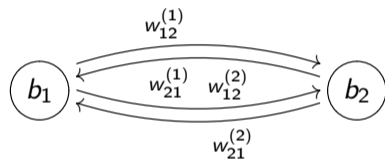
Trade Relation Graph



We model a financial system $FS = (B, \mathcal{L}, \tau)$ as an undirected *trade relation graph*.

- The nodes B represent the banks.
- The multiset \mathcal{L} of all links $\{b_1, b_2\}$ represents the netting sets of all trade relations between them.
- The portfolio of trades $\tau(\ell)\{\mathcal{T}_1, \mathcal{T}_2, \dots, \mathcal{T}_n\} < b_1, b_2 >$ between b_1, b_2 is attached to the link $\ell = \{b_1, b_2\}$ and the color coding represents the asset classes of the trades.

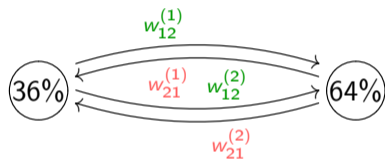
Risk Graph



The *risk graph* $RG = (B, A, w)$ of a trade relation graph $FS = (B, T, \tau)$ is a directed graph.

- The nodes B represent the same banks.
- Each undirected trade relation in ℓ is replaced by two arrows in A between the same nodes in opposite directions.
- $w : A \rightarrow \mathbb{R}^k$ is a weight function representing the risk induced from the tail to the head of an arrow, e.g. $w = \text{EEPE}$ or $w = \text{CVA}$.

Risk Aggregation



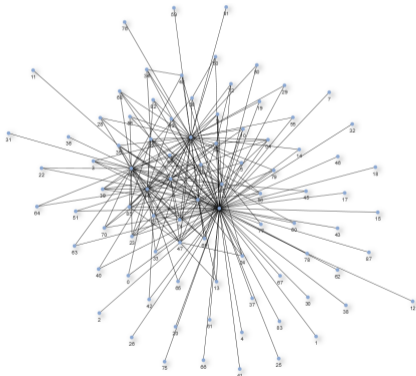
Using a weighted **out-/in-degree** the information in a *risk graph* $RG = (B, A, w)$ can be aggregated from the arrows $a \in A$ to the nodes $b \in B$

$$w^{+/-}(b) := \sum_{\substack{a \in A \\ a \text{ starts / ends at } v}} w(a)$$

and expressed as a percentage of the total of the weight $w(RG) := \sum_{a \in A} w(a)$ via

$$\rho^{+/-}(b) := \frac{w^{+/-}(b)}{w(RG)}.$$

Random Graph Generation



- We start from empirically gained insight that node degree of financial systems is Pareto distributed (core-periphery model).^a
- Generating random graphs with pre-scribed distribution of the node degrees is a difficult problem in discrete mathematics.
- We just use the `configuration_eraser` factory from `networkx` for now.

^ae.g. Cont, R., Moussa, A., and Santos, E. B. (2013). *Network structure and systemic risk in banking systems* in Handbook on Systemic Risk, eds J. Fouque, and J. Langsam (Cambridge: Cambridge University Press), 327–368.

Model Choices

#	aspect	in model
1	repartitioning	✓
2	pre-clearing	✓
3	compression	✓
4	collateral/margining	✗
5	default fund	✗
6	CCP fund	✗
7	non clearing members	✗

- In reality clearing trades does much more than just re-routing them through the CCP.
- We deliberately include only the minimum necessary to study the original idea of central clearing.
- This is to avoid confounding the effects with regulation that could (and sometimes has been) introduced by other means, e.g. collateralization.